

# Uncovering Groups via Heterogeneous Interaction Analysis

---

*Lei Tang, Xufei Wang and Huan Liu*  
Arizona State University



ICDM, Dec. 9th, 2009



YouTube - azcamel007's YouTube - Mozilla Firefox

File Edit View History Bookmarks Digo Tools Help

http://www.youtube.com/

YouTube Broadcast Yourself™ Worldwide | English

(0) azcamel007 Account QuickList (0) Help Sign Out

Home Subscriptions Videos Shows Channels Search Upload

Video File Quick Capture

Try YouTube in a new window Download

**Friend Activity** edit

Your friends haven't done anything yet. Once your friends start uploading, favoriting, and rating videos, we'll show it here on this page. (Can other...)

**Subscriptions** (view all) edit

Your subscriptions haven't added videos lately. When your subscriptions upload and add new videos, we'll show them here on t...

**Recommended for You** (view all) edit

 <p>Backstreet Boys - I want it that... 1 year ago 139,212 views MinekeW ★★★★★</p>	 <p>Back Dormitory Boys 2 years ago 111,987 views SakuraCiel ★★★★★</p>	 <p>two chinese boys:dadada 2 years ago 2,105,378 views younotwolf ★★★★★</p>	 <p>lyrics【歌詞】Bac kstreet 1 year ago 162,404 views monkydance ★★★★★</p>
--	--	---	---

**Videos Being Watched Now** (view all) edit

**Inbox**

- 0 Personal Messages
- 0 Shared with you
- 0 Comments
- 0 Friend invites
- 0 Video Responses

send message

**What's New**

Create, Collaborate, Annotate, and Share with Friends

Watch your favorite videos in HD!

100 Invites to RealTime for Blog Readers  
Today is the beta launch of YouTube RealTime, a new way of discovering what your friends are doing on YouTube. Wanna try it? Be one of the first to comment on this post.  
Read more in our Blog

comment

Video Response

Message

http://www.youtube.com/my\_videos\_upload

facebook | Home - Mozilla Firefox

Edit View History Bookmarks Diigo Tools Help

http://www.facebook.com/home.php

facebook Home Profile Friends Inbox Lei Tang Settings Logout Search

News Feed ASU Public Profiles Photos Links Video More Create

What's on your mind?

Share

Faye Yu seems like everyone is out except from... reviewing the damn AMR paper... and i'm... 2 hours ago · Comment · Like

Faye Yu is not in the vacation... 2 hours ago · Comment · Like

Lawrence Huang at 10:01pm April 23 that is just soooo wrong

Faye Yu at 11:10pm April 23 i agree.

Write a comment...

Kartik Talamadupula Boredom Remedies, #324: My roomie's solution - "surf" BharatMatrimony.com 2 hours ago · Comment · Like

Soujanya Akella at 8:53pm April 23 \*rolling eyes\* good lord.

Show 8 more comments...

Kartik Talamadupula at 10:24pm April 23 Hehe no our man fully busy with classes ... twas Sab ;)

Write a comment...

Suggestions

Susan Boyle Yang Yang Yang is a fan. Become a Fan

Highlights

Simon by Jennifer Thome 5 2

Mobile Uploads by Kartik Talamadupula

Canta Nitin Agarwal commented on this. 1

Life is... by Jiayin Zhang 6

Mobile Uploads

My wedding in Shanghai - 07.15.2005 by Yiyun Zhang

Online Friends (4)

Done

fans

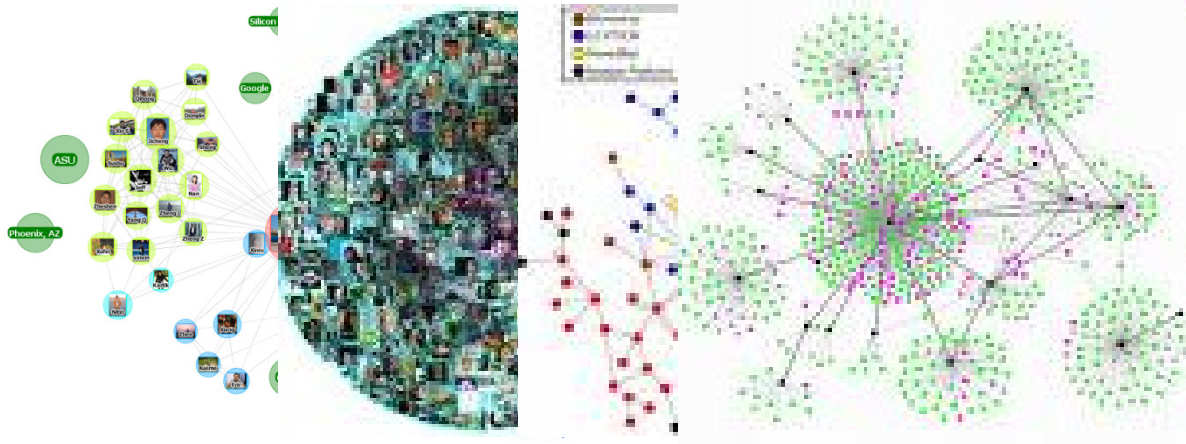
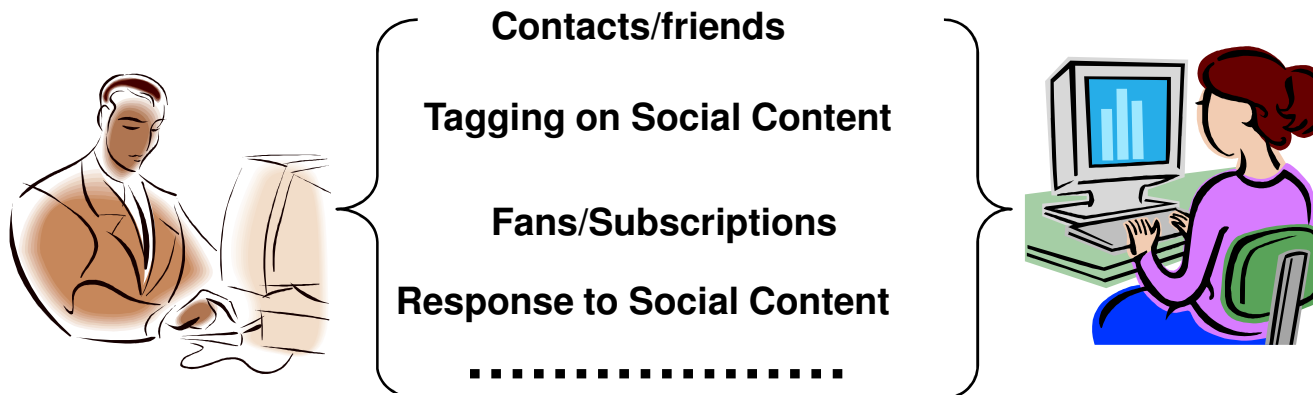
comment

vote

friends

# Multi-Dimensional Network

- Different behaviors lead to **heterogeneous Interactions**



**Network of  
Multiple  
Dimensions**

# Heterogeneous Interaction Analysis

---

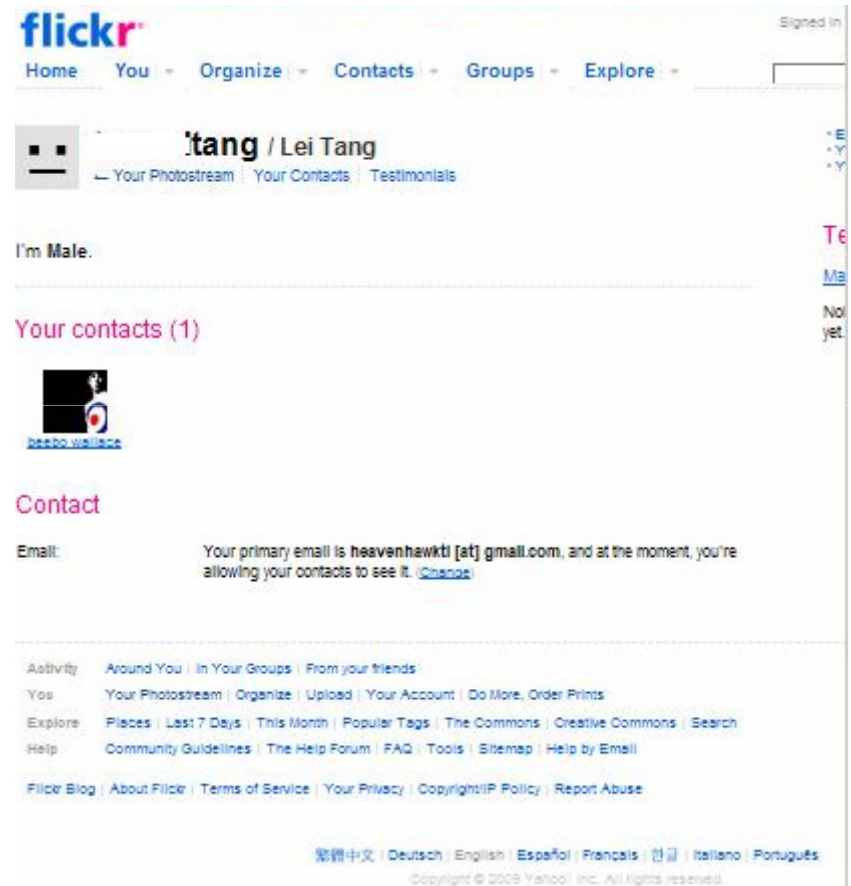
- A latent community structure is shared in a multi-dimensional network
  - E.g. a group sharing similar interest
- Goal: *Find out the shared community structure by integrating the interactions at different dimensions*





# Why not just friends network?

- Too many friends?
- Too few friends?
- Friends network tells limited info for some users
- Interaction at other dimensions might help



# Recap of Modularity

---

- **Modularity:** A measure that compares the within group interaction with uniform random graph *with the same node degree distribution*
- In a network of  $m$  edges, for two nodes with degree  $d_i$  and  $d_j$ , respectively, the **expected number of edges** between them:

$$d_i d_j / 2m$$

- The connection strength in a group:  $\sum_{i \in C, j \in C} A_{ij} - d_i d_j / 2m$
- To partition the network into multiple groups, we maximize

$$\frac{1}{2m} \sum_C \sum_{i \in C, j \in C} A_{ij} - d_i d_j / 2m$$



# Modularity Matrix

---

- Modularity can be formulated in a matrix form

$$Q = \frac{1}{2m} \text{Tr}(S^T B S)$$

- B is the modularity matrix

$$B_{ij} = A_{ij} - d_i d_j / 2m$$

- With spectral relaxation, S corresponds to the top eigenvectors of the modularity matrix B

# Modularity in M-D Networks

---

## □ Average Modularity Maximization (AMM)

- Average the network interaction of different dimensions

$$\bar{A} = \frac{1}{D}(A_1 + A_2 + \dots + A_D)$$

## □ Total Modularity Maximization (TMM)

- the total sum of modularity at different dimensions

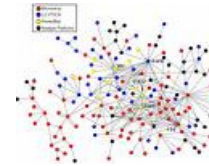
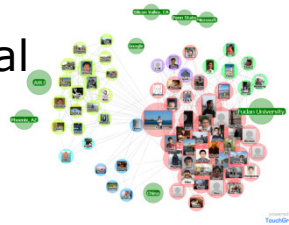
$$\max(Q_1 + Q_2 + \dots + Q_D)$$

## □ Potential Cons

- Not sure whether the interaction or modularity of different dimensions are comparable
- Can be sensitive to networks of noisy dimensions

# Principal Modularity Maximization

Multi-Dimensional  
Networks



Extract **Structural  
Features** via  
Modularity  
Maximization



Denoise the interaction at each dimension

- These structural features are not necessarily similar, but are **highly correlated**.
- Transform these features into **a shared space** such that their correlation is maximized.
- Solution: **Generalized Canonical Correlation Analysis (CCA)**

# Canonical Correlation Analysis

$$R(i, j) = (S_i w_i)^T (S_j w_j) = w_i^T (S_i^T S_j) w_j = w_i^T C_{ij} w_j$$

$$\begin{aligned} \max \quad & \sum_{i=1}^d \sum_{j=1}^d w_i^T C_{ij} w_j \\ \text{s.t.} \quad & \sum_{i=1}^d w_i^T C_{ii} w_i = 1 \end{aligned}$$



$$= \lambda \begin{bmatrix} C_{11} & C_{12} & \cdots & C_{1d} \\ C_{21} & C_{22} & \cdots & C_{2d} \\ \vdots & \vdots & \ddots & \vdots \\ C_{d1} & C_{d2} & \cdots & C_{dd} \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_d \end{bmatrix}$$



$$\begin{aligned} C_{11} &= S_1^T S_1 = I \\ C_{22} &= S_2^T S_2 = I \\ &\dots \end{aligned}$$

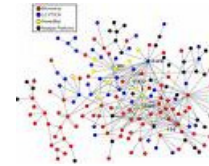
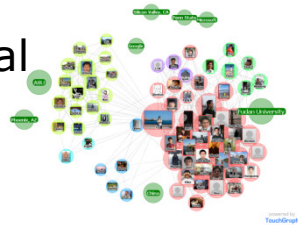
**Principal Component Analysis (PCA)**

eigenvector of the covariance matrix

# Principal Modularity Maximization

---

Multi-Dimensional  
Networks



Extract **Structural  
Features** via  
Modularity  
Maximization

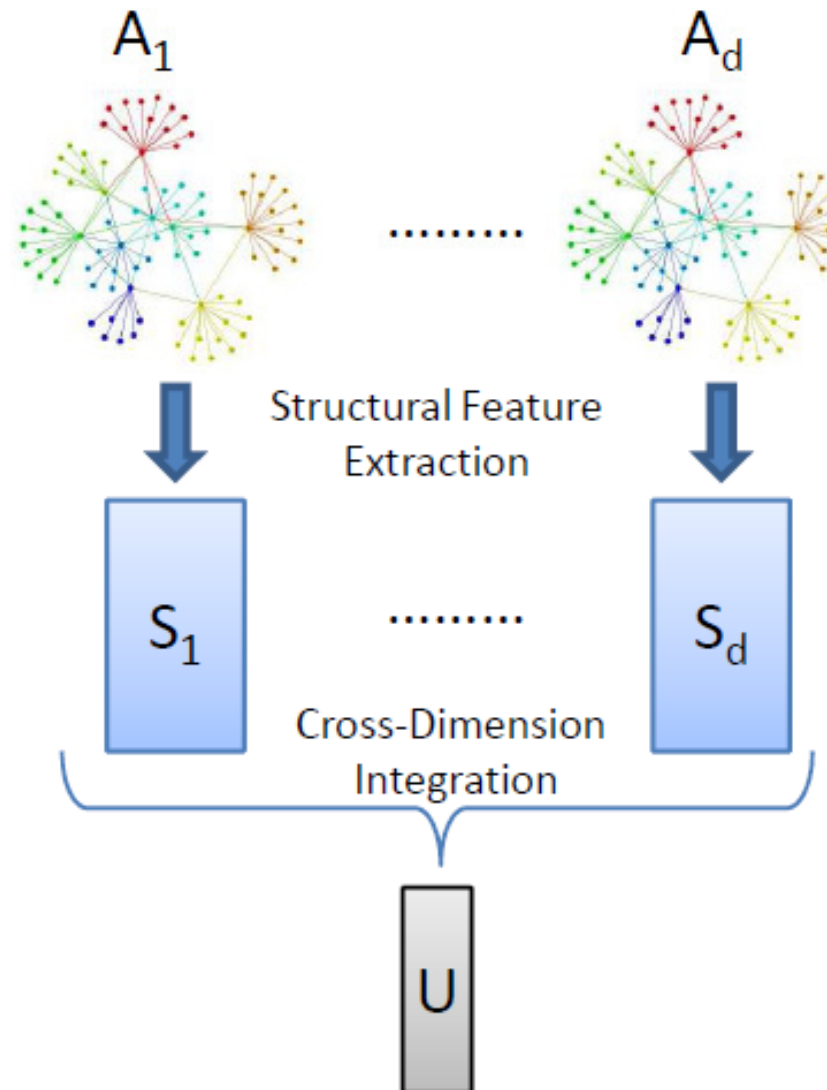


Combine all the structural  
features and perform  
**Principal Component  
Analysis**)



# Overview of PMM

---





# PMM Algorithm

---

- **Given:** a multi-dimensional network
- **Output:** shared group structure
  
- **Algorithm:**
  - **Phase I:** Extract structural features from each dimension of the network
  
  - **Phase II:** Combine all the extracted features of each dimension and perform PCA
  
  - Apply K-means to obtain the discrete partition

# Experiments

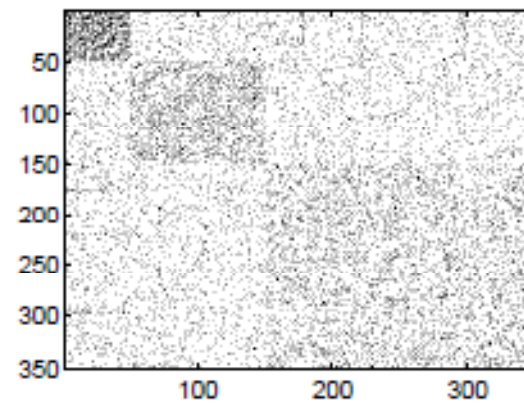
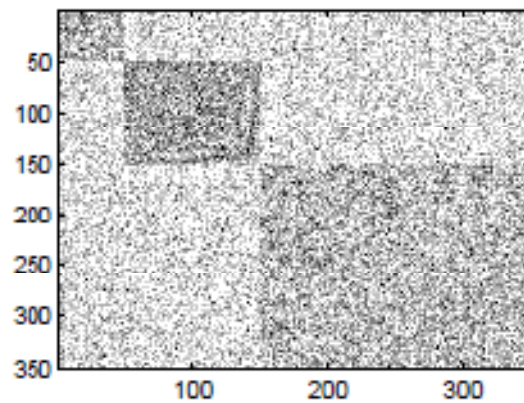
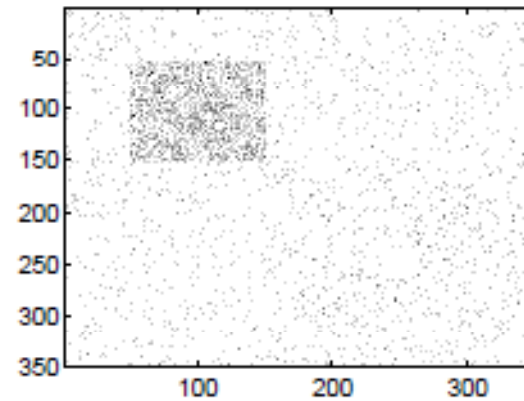
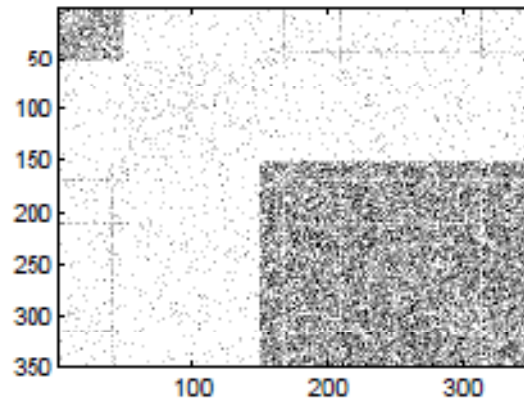
---

- Compare different community detection strategies
  - AMM, TMM, PMM
  - Modularity maximization on a single dimension
- Verify the sensitivity to noise for different methods
- Data Sets
  - Synthetic Data
    - controlled noise and ground truth information
  - Real-World Data
    - collected from YouTube

# Synthetic Data

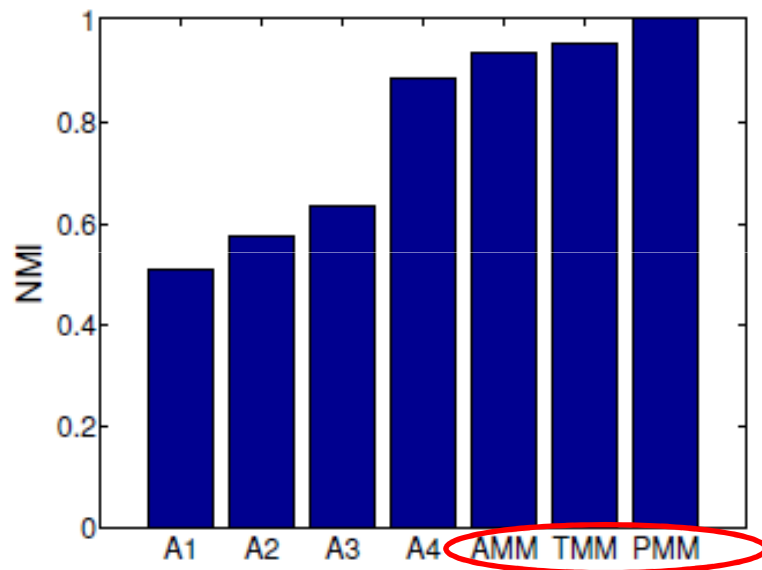
---

- 4 dimensions, 3 communities
- 50, 100, 150 members respectively

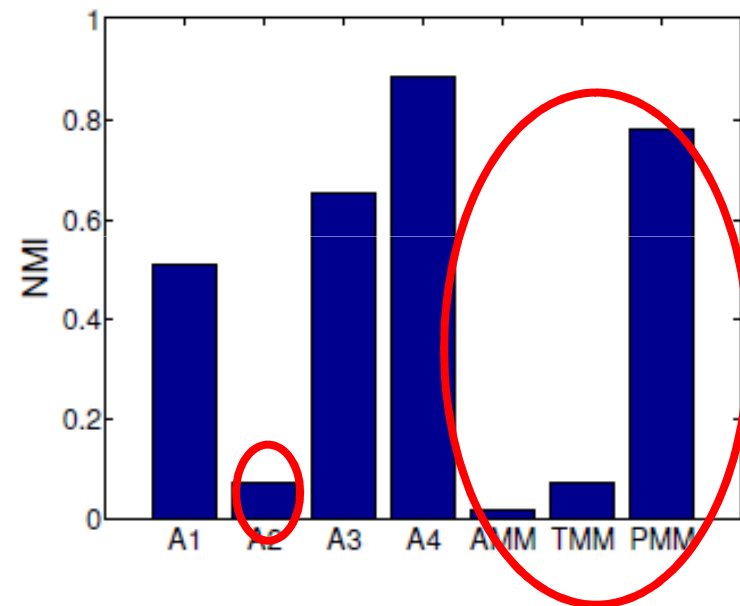


# Performance on Synthetic Data

---



Small Noise



Substantial Noise  
in one dimension

# Average Performance

---

Table 1: Average Performance Over 100 Runs

	Strategy	Performance
Single-Dimensional	$A_1$	$0.7237 \pm 0.1924$
	$A_2$	$0.6798 \pm 0.1888$
	$A_3$	$0.6672 \pm 0.1848$
	$A_4$	$0.6906 \pm 0.1976$
Multi-Dimensional	AMM	$0.7946 \pm 0.1623$
	TMM	$0.9157 \pm 0.1137$
	PMM	<b><math>0.9351 \pm 0.1059</math></b>

Single < AMM < TMM < PMM

PMM: Low Variance

# YouTube Data

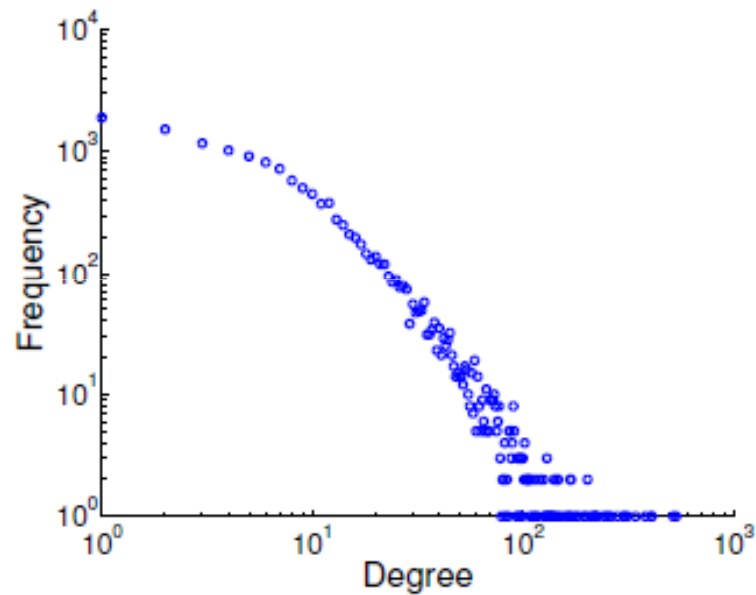
---

- Collect contact network, subscription network, and users' favorite videos
- Crawl 30,522 user profiles reaching in total 848,003 users and 1,299,642 favorite videos
- 15,088 active users
- Construct a 5-dimensional network
  - Contact
  - Share Contacts
  - Share subscription
  - Followed by the same set of people
  - Share favorite videos

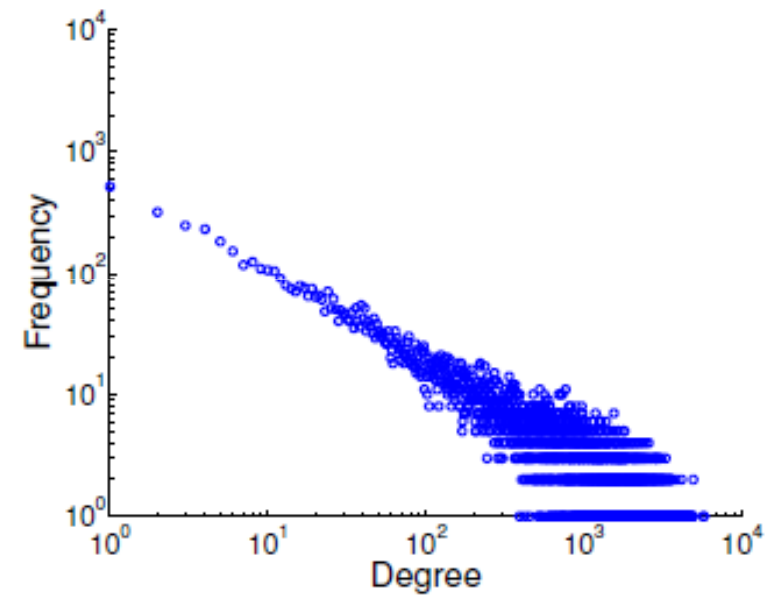


# Degree Distribution

---



(a) Contact Network



(b) Favorite Network

# Evaluation on Real-World Data

---

## □ Challenges

- No ground truth
- Need a smart way to do the comparative study

## □ Evaluation -- Cross Dimension Validation

- Follow the idea of cross validation
- For a network of  $D$  dimensions
  - learn the community structure from  $(D-1)$  dimensions
  - evaluate it on the remaining dimension in terms of modularity

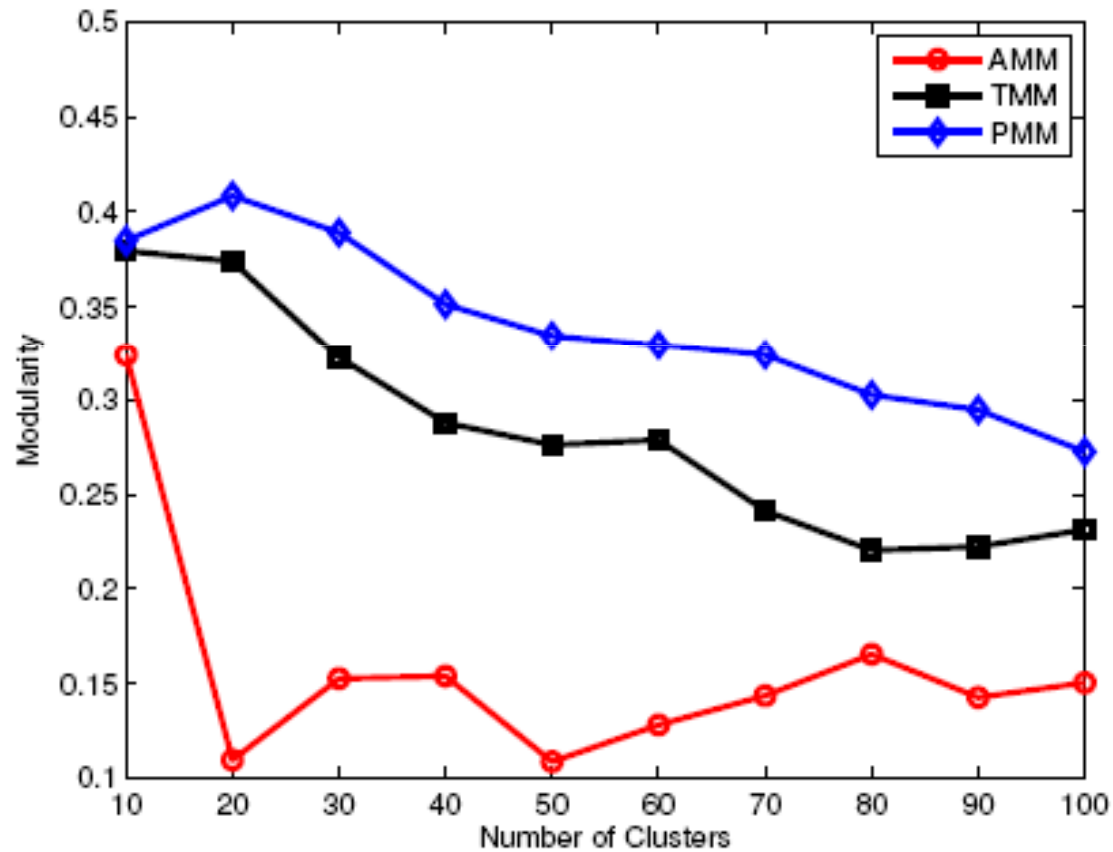
# Performance on YouTube Data

---

Methods	$A_1$	$A_2$	$A_3$	$A_4$	$A_5$
$A_1$	—	.0007	.0008	.0008	.0002
$A_2$	.1548	—	.0133	.0361	.0076
$A_3$	.0712	.0275	—	.0446	.0140
$A_4$	.0584	.0569	.0186	—	.0108
$A_5$	.0314	.0135	.0095	.0180	—
AMM	.1096	.0001	.0018	.0053	.0070
TMM	.3740	.1856	.1246	.1800	.0706
PMM	<b>.4085</b>	<b>.2063</b>	<b>.1307</b>	<b>.1844</b>	<b>.0947</b>

➤ PMM tends to be the winner

# PMM compared with AMM & TMM



AMM < TMM < PMM

# Conclusions & Future Work

---

- Networks in social media are **multi-dimensional** and **noisy**
- Propose an effective **Principal Modularity Maximization** to extract the shared group structure
  - Extract Structural Features via Modularity Maximization
  - Perform Cross-Dimensional Integration via PCA
- Can be applied similarly to other spectral clustering methods
- Future Work:
  - Determine whether two network dimensions share the same community structure?
  - Need to remove noisy interaction dimensions?
  - One actor assigned to multiple different groups?
  - Scalability?

# Acknowledgments

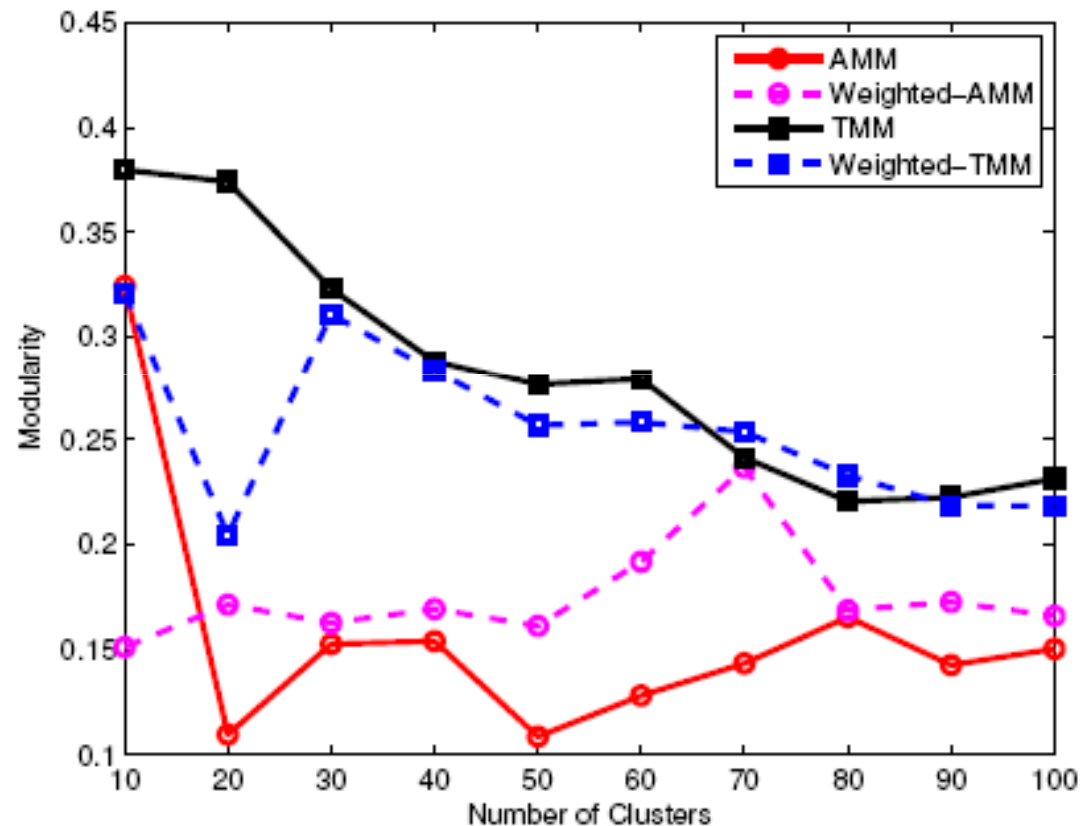
---

- Thanks to the sponsorship of AFOSR and ONR.





# Weighted AMM & TMM



Assigning a proper weight to each dimension is not easy!